# Preliminary Analysis of Stress in the Newberry EGS Well NWG 55-29

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#### Keywords

Geothermal, EGS, image log, fracture, stress, borehole breakout, Newberry

## ABSTRACT

As part of the planning for stimulation of the Newberry Volcano Enhanced Geothermal Systems (EGS) Demonstration project in Oregon, a high-resolution borehole televiewer (BHTV) log was acquired using the ALT ABI85 BHTV tool in the slightly deviated NWG 55-29 well. The image log reveals an extensive network of fractures in a conjugate set striking approximately N-S and dipping 50° that are well oriented for normal slip and are consistent with surface-breaking regional normal faults in the vicinity. Similarly, breakouts indicate a consistent minimum horizontal stress, S<sub>hmin</sub>, azimuth of 092.3 $\pm$ 17.3°. In conjunction with a suite of geophysical logs, a model of the stress magnitudes constrained by the width of breakouts at depth and a model of rock strength independently indicates a predominantly normal faulting stress regime.

## 1. Introduction

Natural fractures play a critical role in developing an Enhanced Geothermal System (EGS) in low permeability to impermeable rock because their combination of slightly greater-than-background permeability and inherent weakness ensures interaction with the stimulation fluids or chemicals. Hydro-shearing takes advantage of these properties to invade the fracture with fluid, thereby reducing the effective normal stress and inducing small slip with the goal of producing self-propping dilation and a tortuous flow pathway (Davatzes and Hickman, 2009 and references therein). Many properties influence the slip behavior, but in this paper we focus on characterizing the natural fracture population in borehole NWG 55-29 in the west flank of Newberry Volcano, OR, and derive a model for the stresses acting on them. The analysis combines constraints from physical property logs including litho-density, neutron porosity, natural gamma, 1-arm caliper, and temperature-pressure-spinner logs and an acoustic borehole televiewer log (BHTV) acquired using the Advanced Logic Technologies (ALT) ABI85 BHTV.

## 2. Geologic Setting

Newberry Volcano is a shield volcano located in the Cascade Range at the intersection of three distinct structural zones: the Cascades Graben, the Brother's Fault zone, and the Basin and Range. Recently acquired LiDAR topographic data in the study area reveals N-S trending normal fault scarps in modern alluvial sediments with only minor variation in strike west of the NWG 55-29 and N-S trending alignments of fissures/vents to the east; both sets of structures indicate E-W extension in the immediate area (Cladouhos et al., 2011a). These structures reflect the geologically recent direction of the least compressive principal stress, S<sub>hmin</sub>, near the Newberry EGS site. This local regional stress orientation is more uniform than might be expected for the Newberry region based on the juxtaposition of three different structural trends.

Petrographic analysis of cuttings from this borehole (Letvin, 2011) and core from the nearby GEO N-2 borehole (Fetterman and Davatzes, 2011) indicate the NWG 55-29 borehole penetrates layers of extrusive volcanic basalt, andesite, rhyolite, and related welded tuffs intruded by granodiorite and dacite below ~8610 ft MD GL (Measured Depth below Ground Level). Multi-stage stimulation is planned in the interval from the casing shoe at 6435 to the total depth at 10040 ft MD GL.

Prior to acquisition of the image log, an inject-to-cool program was initiated to extend the depth of the logged interval to 8860 ft MD below GL at a maximum temperature of 277°C. The resulting log spans the upper 2,425 ft portion of the 3,629 ft open-hole interval.

#### 3.1 Natural Fractures

The BHTV log reveals extensive, shallowly to moderately dipping layering corresponding to volcanic flow boundaries, foliation and lithologic transitions (Figure 1). At approximately 8807 ft MD GL there is a sharp transition to mzassive granodiorite. These volcanic layers are cut by natural fractures with dips consistent with normal slip and similar to dips in core from the



**Figure 1.** Unwrapped images of the Travel Time and Amplitude signals recovered from NWG 55-29. Sinusoidal Natural Fractures (F) are generally subtle, the Lithologic Boundary (L) is indicated by an abrupt transition in amplitude, and breakouts (B) occur as patches of low amplitude (see discussion below). The three dark bands at 120° increments are from the harness that helps secure the piston assembly at the bottom of the ABI85 below the acoustic window to the rest of the tool. These images are in a magnetic north reference frame and depth is relative to the original borehole televiewer log depths, which are 4 ft above ground level.

nearby GEO N-2 corehole at depths down to 4500 ft MD GL. A smaller number of natural fractures occur in the underlying granodiorite.

There are two dominant fracture sets that strike roughly N-S and dip approximately 50° to the east and west, as expected for conjugate normal fractures (Figure 2). The west-dipping set has a greater number of identified fractures, consistent with better sampling due to the slight deviation from vertical of 10.5° to 15.1° towards 086. Poor expression of these fractures in the televiewer log suggests many of them might be at least partially healed.

The thickest, most well-developed fractures are strongly aligned with these average attitudes whereas thinner fractures have a wider distribution of attitudes. However, many of these thick fractures are characterized by either very steep or relatively shallow dips that are inconsistent with normal slip. Given that dips are determined from the boundaries of these thick fractures due to reduced image quality in the fracture interior, their true dip is less certain than for thinner fractures. Dikes have a similar attitude to natural fractures. The attitudes of primary layering such as bedding, the boundaries of volcanic flows, and foliation group into east and west dipping populations similarly to the attitude of natural fractures (Figure 2). However, their dips are generally lower from 10 to 40°. We tentatively interpret this pattern as representing the flanks of ancient cinder cones common in the region (Cladouhos et al., 2011 and references therein). Detailed statistical analysis of the fracture population is discussed in a related manuscript by Cladouhos et al. (2011b).

**Figure 2.** Modified Tadpole plot showing the depth distribution of natural fracture and primary layering attitude. The azimuth of the dip direction is indicated along the x-axis and the tail of the tadpole indicates the dip relative to horizontal. Left: Natural fractures distinguishing undifferentiated fractures, major fractures and minor fractures. Relative thickness is indicated by the symbol size. Center: Natural fracture frequency in 20 ft bins (histogram) and cumulative frequency normalized by the maximum bin frequency. Note that the colors correspond to the categories in the Left panel. Right: Layering distinguishing bedding/banding/foliation, lithologic transitions, and dikes.

#### 3.2 Azimuth of S<sub>hmin</sub> from Borehole Breakouts

Breakouts are patches of the borehole wall 180° apart that undergo compressive failure due to the elastic concentration of effective stresses around a circular borehole (Kirsch 1898; Moos and Zoback, 1990; Zoback et al., 2003; Haimson, 2007). Breakouts were identified in the BHTV log as irregular patches of low amplitude and increased travel time that occur in pairs on diametrically opposed sides of the borehole (Figure 1). If the vertical stress,  $S_{y_2}$ is taken as a principal stress (Anderson, 1951) and is approximately aligned with the borehole axis as indicated by ABI85 and single shot deviation data that range from 10.5° to 15.1° in the interval of the BHTV log, then breakouts are oriented along the minimum horizontal principal stress (S<sub>hmin</sub>) azimuth (Plumb and Hickman, 1985; Moos and Zoback, 1990; Peska and Zoback, 1995; Zoback et al., 2003). Following the method of Davatzes and Hickman (2010a and b), the orientation of  $S_{hmin}$  was determined from the breakouts weighted by their vertical extent in the borehole.

Clearly defined breakouts are distributed throughout the image log in the volcanic materials above 8610 ft MD GL, but are absent in the underlying granodiorite. These breakouts show a consistent azimuth independent of borehole deviation and indicate that the  $S_{hmin}$  azimuth is 092.3 ± 17.3°. As discussed in detail below, this azimuth of  $S_{hmin}$  in combination with the attitude of the majority of natural fractures revealed in the BHTV log is consistent with normal faulting (Figure 2).

#### 3.3 Principal Stress Magnitudes

The stress tensor acting on the volume containing NWG 55-29 should be completely characterized by the vertical principal stress



**Figure 3.** Statistics of breakout occurrence in borehole NWG 55-29. Left panel shows the vertical distribution of breakouts versus measured depth, where horizontal bars indicate breakout width, red breakouts correspond to high quality picks of paired breakouts and blue breakouts are lower quality picks of single breakouts that typically occur in areas of poor image quality. Vertical yellow-filled boxes show the mean  $S_{hmin}$  azimuth  $\pm$  one standard deviation as calculated using circular statistics and weighted by the vertical extent of individual breakouts. The upper right histogram shows the distribution of breakout widths. The Lower right rose diagram summarizes the cumulative height in feet of breakouts in 10° azimuthal bins.

and two horizontal principal stresses, all of which are counteracted by the formation fluid pressure through the effective stress principle. In this section, we model each of these four components to determine the effective stress tensor. This includes constraints on the magnitudes of horizontal principal stresses derived from the injection history, borehole deformation, and strength limits of the rock that the borehole penetrates.

#### 3.3.1 Vertical Principal Stress and Fluid Pressure

We calculate the vertical stress  $(S_V)$  using a geophysical lithodensity log spanning 332.5 m (1091 ft) below GL to a depth of 3066.3 m (10,040 ft) MD GL and an estimated average density for the overlying interval. The log data were filtered to remove spurious bulk density measurements in cases where the bulk density correction exceeds 0.2 g/cc (Asquith and Krygowski, 2004) or where the 1-arm caliper showed extensive washout. Geophysical measurements of bulk density are consistent with the bulk density estimated from the weighted average of the mineralogy measured through Rietveld Refinement of XRD of cuttings corrected for water-filled porosity using the neutron porosity log. The litho-density log data and the variation in  $S_v$  with depth calculated from these data are shown in Figure 4.

The undisturbed formation fluid pressure was derived from two equilibrated pressure logs: one on October 3, 2008, approximately 2.5 months after the borehole was completed, and a subsequent pressure log conducted September 22, 2010, prior to the inject-to-cool preparations for BHTV logging. As shown in Figure 4, the first of these logs was conducted when the borehole was open to the atmosphere, and reflects a static water table at 420 ft (128 m) TVD GL.

#### 3.3.2 Constraints on the Minimum Horizontal Principal Stress, S<sub>hmin</sub>

In most stress analyses carried out in geothermal systems, we measure the magnitude of  $S_{hmin}$  directly using a mini hydraulic fracturing test (see Hickman and Davatzes, 2010b, and references therein for details) and then constrain the magnitude of  $S_{Hmax}$  using observations of breakout width and estimates of UCS,  $P_f$  and



**Figure 4.** Analysis of stresses versus depth for borehole NWG 55-29, *assuming a variable UCS*. From left to right: *Panel 1:* Fractional porosity (green) and raw bulk density (red), filtered bulk density (blue) and filtered and then smoothed bulk density (black) from the litho-density log. *Panel 2:* Average width of pairs of high-quality breakouts. *Panel 3:* UCS modeled from filtered neutron porosity (red) and UCS values used to model S<sub>Hmax</sub> from breakout width (blue dots). *Panel 4:* Vertical stress profile with estimates of S<sub>Hmax</sub> assuming S<sub>hmin</sub> corresponds to the critical magnitude for normal faulting for  $\mu_s = 0.55$  and allowing for variable UCS as derived from panel to the left (blue dots). For comparison, dashed black lines show S<sub>Hmax</sub> for a variety of constant UCS models. *Panel 5:* Vertical stress profile assuming S<sub>hmin</sub> corresponds to the critical magnitude for normal faulting at  $\mu_s = 0.70$  using variable UCS as in the panel to the left. The thick vertical line indicates the extent of casing. In Panels 4 and 5, the black triangles correspond to the subset of S<sub>Hmax</sub> magnitudes derived from breakout width consistent the assumption of a volume critically stressed for normal faulting. This subset is used to estimate a gradient in S<sub>Hmax</sub> in the image logged interval.

P<sub>m</sub> (e.g., Davatzes and Hickman, 2006). Because reliable and safe open-hole packers do not presently exist for use at temperatures typical of geothermal wells, these mini-frac tests are usually carried out in a short (~50 ft (15.2 m)) and relatively impermeable section of well bore drilled just below a cemented casing shoe. Because NWG 55-29 has over 1000 m (>3000 ft) of open hole and isolating a short section of the hole (e.g., through sanding and cement plug-back procedures) would require a drilling rig, it is not feasible to conduct a mini-frac to determine S<sub>hmin</sub> prior to stimulation due to timing and budgetary constraints. However, step-rate injection tests during the early stages of the EGS stimulation in NWG 55-29, with downhole pressure and temperature profile monitoring, will be used to provide direct constraints on the magnitude of S<sub>hmin</sub> and depth of hydrofrac initiation, if it occurs. In addition, we will be carrying out mini-frac tests during drilling of the Newberry EGS production well during a later phase of the project, employing the procedures outlined above.

Although we currently lack a direct measurement of S<sub>hmin</sub>, previous injection tests do constrain Shmin. During the inject-to-cool operation prior to BHTV logging (Table 1), temperature-pressure logs were conducted at well head pressures (WHP) of 640 psi and 785 psi and provide complete records of pressure and temperature variation at depth (Figure 4). In another phase of the same operation, although no temperature-pressure log was obtained, maximum WHP reached 1153 psi. This WHP was achieved over three days prior to running the temperature-pressure log at 785 psi, so the downhole pressures corresponding to a WHP of 1153 psi are estimated by shifting the measured pressure profile during the 785 psi WHP survey to bring it into alignment with the maximum WHP of 1153 psi. This adjusted injecting  $P_f$  profile is plotted in Figure 4, Panel 3 and 4. In spite of the high borehole fluid pressures attained, these injection tests did not result in hydrofracture as indicated by a lack of change in injectivity (Table 1), a lack of either pressure or temperature signatures in concurrent temperaturepressure logs (personal comm., L. Nofziger, 2011), and the lack of tensile fractures visible anywhere in the BHTV log. In addition, the apparent injectivities during this operation are similar to those measured in other un-stimulated boreholes at Newberry, including CEE 76-15 TCH, CEE 86-21 and CEE 23-22 (Spielman and Finger, 1998). Since hydrofracs form in response to borehole fluid pressure in excess of S<sub>hmin</sub>, the failure to create a hydrofrac during this inject-to-cool operation provides a lower bound to the magnitude of  $S_{hmin}$ . Thus,  $S_{hmin}$  within the open-hole interval of NGW 55-29 must lie to the right of the dashed magenta line in Panels 3 and 4 of Figure 4, or else hydraulic fracturing would have occurred.

 Table 1. Apparent injectivity in NWG 55-29 from wellhead pressure and injection rates.

	Log Date	Well-Head- Pressure (WHP)	Injection Rate	Pressure Log	Duration	Apparent Injectivity
		[psi]	[gpm]		[gpm/psi]	
	2010-09-24 to 27	751	10	No	3 Days	0.013
	2010-09-27	619	13	Yes		0.021
		821	17		Short-term	0.021
	2010-10-11 to 20	1153	22	No	9 days	0.019
	2010-10-20	785	13	Yes	Short-term (conducted during logging after 1153 psi WHP)	0.017

Another approach is to explore additional limits on  $S_{hmin}$  derived from a combination of an assumed tectonic environment and the frictional strength of the crust. As discussed above, it is reasonable to assume a normal faulting environment at Newberry based upon the attitude of the preponderance of natural fractures seen in the BHTV log, mapped faults at the surface, and the similarity of the  $S_{hmin}$  azimuth to the dip direction of these structures. In such a normal faulting environment, the maximum differential stress a rock can sustain is given by the difference between  $S_v$  and  $S_{hmin}$ , assuming there is a population of optimally oriented, cohesionless fractures. In accordance with the Coulomb failure criterion, frictional failure (i.e., normal faulting) would then occur at a critical magnitude of  $S_{hmin}$  given by (after Jaeger and Cook, 1979):

$$S_{hmin}^{crit} = (S_V - P_f) / [(\mu_s^2 + 1)^{1/2} + \mu_s]^2 + P_f$$
(1)

where  $\mu_s$  is the static coefficient of friction of preexisting faults. Mineralogy from cuttings indicates that  $\mu_s$  might range from an extreme low of 0.38, consistent with the coefficient of friction of chlorite as the weakest mineral found in the cuttings (Lockner and Beeler, 2002) to 0.85, consistent with a representative rhyolite tuff from another locality (i.e., the paintbrush tuff in the vicinity of Yucca Mountain, NV, Morrow and Byerlee, 1984). In general, laboratory sliding experiments on a variety of rock types show average behavior  $\mu_s \sim 0.75$  to 0.90 (Byerlee, 1978), but lower  $\mu_s$ of 0.55 to 0.6 is also common (Jaeger and Cook, 1979; Paterson and Wong, 2005). Similar constraints on frictional strength have been derived from extensive in situ stress measurements in a wide range of tectonic environments (e.g., Townend and Zoback, 2000) as well as in other geothermal fields (Barton et al., 1998; Hickman et al., 1998, 2010; Davatzes and Hickman, 2006, 2010b; Cornet et al., 2007; Valley and Evans, 2007; Hickman and Davatzes, 2010) and support the idea that differential stress levels in the crust are generally limited by  $\mu_s \sim 0.6$  to 1.0. To provide frictional bounds on Shmin in the vicinity of hole NWG 55-29, we use Eq. 2 to calculated  $S_{hmin}^{crit}$  corresponding to  $\mu_s$  ranging from 0.38 to 0.85 (Figure 4).

## 3.3.3 Constraints on the Maximum Horizontal Principal Stress, S<sub>Hmax</sub>

As noted earlier, breakouts span portions of the borehole wall where the compressive normal stress tangential to the borehole wall exceeds the compressive strength of the rock (see Zoback et al., 2003; Haimson, 2007). The variation of the stress components along the borehole wall is described by the 2D plane strain Kirsch equation (Kirsch, 1898). Additional sources of stress at the borehole wall include formation pore fluid pressure ( $P_f$ ), the

pressure difference between  $P_f$  and the fluid pressure in the borehole ( $P_m$ ), and thermal stresses induced at the borehole wall by circulation of hot or cold fluids (e.g., during drilling). Following Zoback et al. (2003), the Kirsch equation is modified to include all of these contributions to the stresses causing breakout formation:

$$\sigma_{\theta\theta} = S_{Hmax} + S_{hmin} - 2(S_{Hmax} - S_{hmin})\cos(2\theta) - 2P_{f} - \Delta P + \sigma^{thermal}$$
(2)

Where  $\sigma_{\theta\theta}$  is the tangential circumferential normal stress at the borehole wall,  $\theta$  is the angle measured from the  $S_{Hmax}$  azimuth, and  $\Delta P$  is the difference between

the mud pressure and the formation fluid pressure, such that  $\Delta P = P_m - P_f$ . In this formulation, positive  $\Delta P$  adds a component of tensile circumferential stress at the borehole wall. The term  $\sigma^{\text{thermal}}$  refers to thermal circumferential stresses induced by heating or cooling the borehole wall.

Since the borehole wall is in contact with the borehole fluid and the pore pressure in rock immediately outside the borehole during breakout formation is assumed approximately equal to the borehole fluid pressure, the appropriate strength criterion for breakout formation is the uniaxial compressive strength (UCS; see discussion in Zoback et al., 2003, Zoback, 2007, and Haimson, 2007). For breakout formation, the maximum value of circumferential stress is aligned with the S<sub>hmin</sub> azimuth, where  $\theta$  in Eq. 2 is either 90° or 270°. Breakout width (wBO) is defined as the angle subtended by the breakout at the borehole wall and corresponds to the condition at which  $\sigma_{\theta\theta} \ge UCS$ .

UCS typically varies by at least three orders of magnitude and as many as six orders of magnitude in volcanic rock (Price et al., 1993; Li and Abertson, 2003; Ma and Daemen, 2004; Entwisle et al., 2005; Frolova et al., 2005), thus large variations in breakout width can occur at constant differential stress. UCS depends strongly on the internal structure of materials, and in particular on the distribution of flaws that can locally concentrate stress and initiate failure (Lawn, 1993; Quane and Russel, 2003; Li and Albertson, 2003; Hudyma et al., 2004; Paterson and Wong, 2005). Total porosity, pore shape, and to a lesser degree, pore size impact the magnitude of the stress concentration and thus have the strongest impact on the strength of the rock. In volcanic rocks, there can be a high degree of variability in pore size and shape due to the presence of two distinct pore populations: (1) small, sharp microcracks resulting from cooling stress, burial, and tectonic activity, and (2) potentially large, rounded vesicles that form during solidification from a melt and exsolution of volatiles.

Numerous studies have demonstrated a good empirical correlation between porosity and UCS for a variety of rock types (Ryshkewitch, 1953; Duckworth, 1953; Rzevsky and Novick, 1971; Dunn et al., 1973; Price et al., 1993; Moos and Pezard, 1996; Li and Aubertin, 2003; Kleb and Vasarhelyi, 2003; Ma and Daemen, 2004; Entwisle et al., 2005; Ma et al., 2006; Zoboack, 2007). To allow for variations in UCS within the open-hole interval of NWG 55-29, we compiled UCS and porosity data (Figure 5) on relevant rock types to derive an empirical strength model by least squares fitting of an exponential function as follows:

$$UCS = 13800 \exp(-0.04744\phi)$$

where porosity,  $\phi$ , is in percent. In this empirical model the fitting constant in the exponential term was derived from laboratory determinations of UCS versus porosity for numerous rocks with lithologies similar to those encountered in NWG 55-29 and the pre-exponential term was chosen to pass through the UCS magnitude determined from the only available complete failure envelope for welded tuff from nearby well GEO-N2 at 4281 ft MD (Ahmad Ghassemi, pers. comm, 2011). The model was then used to estimate in situ strength in NWG 55-29 from the neutron porosity log (NPHI; see Figure 4). The borehole compensated neutron porosity log measures the total porosity of the rock by direct interaction of neutrons with hydrogen atoms primarily associated with water molecules between a source and a detector, without regard to pore shape or whether the water is structured in a mineral (Hearst et al., 2000). We note here that X-Ray Diffraction and petrographic analysis of the cuttings in the logged interval (not presented) reveals a lack of expandable clays and only a small weight percent of zeolites in the logged interval, suggesting this log accurately represents the in situ porosity.



**Figure 5.** Compiled strength data and fits of fit types identified in the literature to the composite data set. The form of the correlations most commonly including power law (Rzevsky and Novick, 1971; Novik,1978; Price et al., 1993; Moos and Pezard, 1996), exponential (Ryshkewitch, 1953; Duckworth, 1953; Kleb and Vasarhelyi, 2003; Ma and Daemen, 2004; Entwisel et al., 2005; Ma et al., 2006; Zoboack, 2007), and critical porosity models derived from fracture mechanics principles (Dunn et al., 1993; Li and Aubertin, 2003). The exponential fit provided the most satisfactory representation.

(3)

We explored two models for the magnitude of S<sub>Hmax</sub> derived from individually measured breakout widths, the UCS at corresponding depths calculated from porosity (Eq. 3), and assuming that the magnitude of Shmin was controlled by optimally oriented, critically stressed fractures with coefficients of friction of 0.55 and 0.70 (Figure 4). With these parameters,  $S_{Hmax}$  is derived from breakout width by using the conditions most favorable to their formation between when the borehole was drilled and when it was logged, which in the NWG 55-29 borehole includes: (1) minimum borehole fluid pressures given by the equilibrated fluid pressure profile (since excess borehole fluid pressure contributes tension to  $\sigma_{\theta\theta}$  that inhibits breakout formation) and (2) zero stress due to cooling, in effect neglecting the thermal stress term in Eq. 2 (which would contribute a tension to  $\sigma_{\theta\theta}$  that would also inhibit breakout formation). For this analysis, we filtered the more complete breakout data set to base the model solely on the average width of breakouts that occur in distinct pairs and UCS estimates based on porosity values filtered to account for adverse borehole logging conditions such as stand-off as revealed by analysis of the 1-arm caliper log.

Under these assumptions, the majority of breakouts suggest that S<sub>Hmax</sub> is less than S<sub>V</sub> throughout the open-hole interval (Figure 4), which is consistent with geologic evidence discussed above suggesting that this site is in a predominately normal faulting stress regime. For either S<sub>hmin</sub> profile, magnitudes of S<sub>Hmax</sub> that exceed S<sub>V</sub> in this model lie outside the frictional bounds on stress for normal slip and likely reflect variations in rock strength that are not accounted for in the strength model. In other words, low UCS can account for wide breakouts without invoking excessive  $S_{Hmax}$  magnitudes. We also solved Eq. 2 to define contours of  $S_{Hmax}$ as a function of UCS for a single breakout width representative of the entire population, using the statistical mode for wBO of  $35.86^{\circ}$ . In this approach the slope of the S<sub>Hmax</sub> model depends on the corresponding variation in Shmin and Pf, whereas the magnitude of UCS relative to a constant breakout width determines the intercept. Alternatively, the crust could be under-stressed with respect to  $S_{hmin}$ , in which case  $S_{hmin}$  would be greater than expected from Eq. 1, allowing the magnitude of  $S_{Hmax}$  to lie within the strikeslip faulting regime (i.e.,  $S_{Hmax} > S_v$ ) while still not exceeding the frictional strength of the crust.

#### 3.3.4 Complete 3D Stress Model

The stress polygon in Figure 6 serves to summarize the analysis of stress magnitudes in the open-hole interval of NWG 55-29 and review combinations of horizontal principal stress magnitudes consistent with the constraints derived from borehole fluid pressure, rock strength, and breakouts (Jaeger and Cook, 1979; Moos and Zoback, 2000; Zoback, 2007). The edges of the polygon are determined from Eq. 1 for given  $P_f$  and  $\mu_s$  at a depth corresponding to an interval of high fracture density at 8420 ft MD GL (Figure 2) assuming optimally oriented fractures are present in the stressed volume. Combinations of the principal stresses contained within the polygon can be supported by the frictional strength of the surrounding crust. The relative magnitudes of  $S_{hmin}$  and  $S_{Hmax}$  to  $S_V$  also determine the type of fault slip that should predominate: normal, strike slip, or reverse.

In addition, combinations of  $S_{hmin}$  and  $S_{Hmax}$  consistent with the statistical mode of the mapped breakout width for different

UCS are projected into the stress polygon as a series of contours. Smaller UCS magnitudes reduce the  $S_{Hmax}$  necessary to yield this representative breakout width and allow more potential combinations of  $S_{hmin}$  and  $S_{Hmax}$  within the normal faulting stress regime (Figure 6). Since the circumferential compressive stress leading to breakout formation ( $\sigma_{\theta\theta}$ ) *increases* rapidly with increasing  $S_{Hmax}$ , whereas increases in  $S_{hmin}$  cause a relatively small *reduction* in  $\sigma_{\theta\theta}$  (Eq. 1), the slope of these contours is only at a small positive angle to the  $S_{hmin}/S_v$  axis. Thus, for a given rock strength and breakout width, relatively small increases in  $S_{Hmax}$  are required to counteract large increases in  $S_{hmin}$ . This explains the small differences in calculated  $S_{Hmax}$  magnitudes corresponding to  $S_{hmin}$ models in which  $\mu_s = 0.55$  versus  $\mu_s = 0.7$  (Figure 4).

From this analysis, three distinct stress states can be distinguished within the current constraints (Table 2): (1) the volume is critically stressed for normal faulting, (2) the volume is criti-



Figure 6. Stress polygon showing bounds on principal stress ratios for normal faulting, strike-slip and reverse faulting stress regimes permitted by a  $\mu_s$  of 0.7 at a depth of 8420 ft MD GL. The best estimate of stress magnitudes at this depth is for  $S_{hmin}^{crit}$  in frictional equilibrium with  $\mu_s$ =0.55 and corresponding estimates of S<sub>Hmax</sub> from individual measurements of breakout width and a porosity-dependent UCS. Combinations of  $S_{hmin}\xspace$  and  $S_{Hmax}\xspace$  consistent with the statistical mode of measured breakout widths can be traced for specified magnitudes of UCS along the colored sloping lines. Three potential ranges of horizontal principal stress are distinguished: (1) Normal Faulting (red), (2) Strike Slip Faulting (yellow), and (3) a system that is either normal or strike slip, but is under-stressed even for coefficient of friction,  $\mu_s < 0.4$  (gray). Diamonds show possible stress states when Shmin is at frictional equilibrium with the coefficients of friction shown, with  $S_{Hmax}$  derived from the statistical mode of wBO and using the porosity-dependent UCS appropriate to this depth (~10,000 psi; see Figure 4). Triangles indicate stress constraints for breakouts, assuming S<sub>hmin</sub> in equilibrium with  $\mu_s = 0.55$  and with  $S_{Hmax}$  determined using individual measurements of wBO and porosity-dependent UCS. These stress states either lie within the stress polygons for normal or strike-slip faulting (as indicated) or exceed the frictional strength of the crust in a strike-slip faulting stress regime (non-physical case).

Table 2. Characteristics	of	Permissible	Stress	Regimes.
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Stress Case	Pros	Cons	
Characteristics	• $P_f/S_v \approx 0.34$ in the open hole	• No unique constraints on horizontal	
common to all	+ $S_{hmin}profile$ lies above greatest injection pressure profile	principal stresses (especially $S_{h\min})$	
stress cases	• Reverse faulting is incompatible with regional tectonics		
NF (nearly critically stressed)	• Frictional failure occurs in the range $\mu_s = 0.4$ to 0.6	• Requires relatively low static friction compared to mineralogy, Byerlee's Law or Yucca Mtn. Tuff to be cur- rently active	
	• Compatible with the majority of mapped regional faults and fractures revealed in the BHTV log		
	• Compatible with the most common (statistical mode) wBO measurements and variable-UCS stress model		
	• Consistent with small variation in azimuth of breakouts		
SSF (nearly	• Frictional failure occurs in the range of $\mu_s = 0.4$ to 0.6	<ul> <li>Requires high average UCS to explain predominately low wBO if SHmax &gt; Sv</li> <li>Not consistent with most faults mapped</li> </ul>	
critically stressed)	$\bullet$ Compatible with high magnitudes of $S_{\rm Hmax}$ predicted from some wBO measurements and variable-UCS		
	stress model		
	Consistent with small variation in azimuth of breakouts	at surface or seen in BHTV log	
Stable	Consistent with lack of seismicity	None. This is the most likely stress	
(Under- stressed)	• Allows for expected ranges of rock $\mu_s$ = 0.65-0.85, without violating lower bound on $S_{\rm hmin}$ imposed by inject-to-cool operations	case, although the crust could be only slightly removed from criticality (see text). Consistent breakout azimuth requires $S_{hmin}$ cannot approach the magnitude of $S_V$ Note that the mostly likely range of	
	Average UCS to explain individual wBO measurements most consistent with a NF or transitional NF-SSF stress state		
	• NF stress state consistent with range of regional fault and borehole fracture attitudes	UCS is from 8,000 to 12,000 psi	

ability in wells was low when individual fractures as well as the overall fault zone hosting the geothermal field were not critically stressed for friction failure (Hickman et al., 1998; Barton et al., 1998). However, the extent of this under-stressing was small, and mini-hydraulic fracturing tests still showed significant differential stresses, even in very low-permeability wells.

Most of the potential combinations of horizontal principal stresses lie within the normal faulting stress regime (Figure 6), especially when considering the probable magnitudes of UCS, which range from 6,000 to 12,000 psi in the open hole interval and average ~10,000 psi at the modeled depth (Figure 4). Although the three possible stress states listed in Table 2 are not distinguishable without additional constraint provided by a direct measurement of S<sub>hmin</sub> from a mini-hydraulic fracturing

cally stressed for strike slip faulting, and (3) the volume is under stressed. In the normal faulting case, the  $S_{hmin}$  profile lies above

the maximum injection pressures and in the range consistent with frictional failure at 0.6 to 0.4, below the transition to strike slip faulting consistent with the most common fault orientations mapped regionally and with fractures identified in the borehole, and consistent with breakout occurrence using the typical range of porosity-dependent UCS. The strike slip faulting case requires high average UCS to explain the most common breakout widths and is not consistent with most mapped faults and fractures, but is otherwise similar to the normal faulting case. In the case of an under-stressed volume, the stresses are insufficient to cause slip on rocks of typical frictional strength under ambient fluid pressure conditions. This case is consistent with an over-all lack of seismicity and the absence of distinct stress rotations in the BHTV log (which would indicate localized stress rotations due to fault slip) and potentially with low permeability related to high proportions of healed (sealed) fractures. Regarding this later possibility, previous studies in a fault-hosted geothermal field at Dixie Valley, NV, showed that permetest, the under-stressed (or slightly under-stressed) NF case is probably the most likely. However, although a lack of seismicity



**Figure 7.** Slip tendency determined by the ratio of resolve shear to effective normal stress of natural fractures (left) and primary layering (right) versus depth based on a constant gradient in P<sub>p</sub>, S<sub>hmin</sub>, S<sub>v</sub>, S<sub>Hmax</sub> for the open hole interval (Figure 4). Note that in this case the profiles of the principal stresses and fluid pressure are not forced through the origin and thus honor the stress magnitude model.

may be *consistent* with an under-stressed crust at this location, it is important to note that areas known to be critically stressed from extensive mini-hydraulic fracturing tests can be seismically quiescent, especially in areas of low tectonic stressing rates (e.g., Stock et al., 1985; Hickman et al, 1998). Furthermore, the great majority of sites in which in situ stresses have been measured directly, even in stable continental interiors, are critically stressed or near critically stressed (Townend and Zoback, 2000). Thus, the horizontal differential stresses at this site might be as large as indicated in our critically stressed NF stress model (for  $\mu_s \sim 0.55$ ), which would induce shear reactivation along well-oriented faults with only a modest increases in fluid pressure. Finally, relatively high horizontal differential stresses are consistent with the observation that breakouts in well NWG 55-29 are strongly developed and uniformly oriented (e.g., Figure 3), in spite of localized variations in rock fabric, fracturing, or dikes, which might otherwise be expected to lead to local scatter in breakout azimuths (Blake and Davatzes, 2011 and references therein).

## 4. Interaction of Stresses and Natural Fractures

The relative potential for slip of the natural fracture population (Figure 2) is determined by the frictional resistance of these structures, which is given by the ratio of shear to effective normal traction. This ratio is sometimes called the slip tendency, and is presented in Figure 7 assuming a stress model that is slightly under-stressed for frictional failure as given by an Shmin in which the most stressed fracture has an effective slip tendency of 0.55, which means that if its  $\mu_s$  is lower than 0.55 it could slip. With the current constraints on stress magnitudes, we are unable to distinguish precisely how much shear stress is available to drive slip. Nevertheless, if normal faulting predominates, this model does show: (1) slip tendency in excess of  $\sim 0.7$  is not possible given constraints on the mean and differential stress (Figure 4); (2) that the same range of slip tendency occurs throughout the borehole; (3) most of the thickest fractures are under-stressed for normal slip (and strike slip); (4) most of the primary lithologic structures are less stressed than the natural fracture population.

The apparent stability of fractures in this interval is consistent with the overall lack of permeability in the borehole, since low rates of reactivation imply that permeability regeneration accompanying shearing of these fractures cannot keep up with the rate of healing (Barton et al., 1998). This interpretation is consistent with the extensive healing of fractures found in shallower core (<4500 ft) available in the GEO N-2 corehole (Fetterman and Davatzes, 2011). However, the stress model does require significant differential stress between  $S_V$  and  $S_{hmin}$  as well as between  $S_{hmin}$  and  $S_{Hmax}$ . Thus, sufficient shear stress is available to induce slip if the fluid pressure is raised (e.g., Figure 7) as part of hydraulic stimulation, whereas the overall low mean stress should facilitate dilation during slip (Jaeger and Cook, 1979; Heffer, 2002).

## 5. Conclusions

Analysis of the vertical stress from the litho-density log, of formation fluid pressure from the equilibrium fluid pressure logs, and of breakouts visible in the image log suggest a tendency for a normal faulting stress regime consistent with the attitude of imaged natural fractures and faults mapped at the surface. Fractures occur throughout the image-logged interval including fractures well oriented for normal or oblique-normal slip given the azimuth of  $S_{hmin}$  is 092.3±17.3° as derived from breakouts. Strike slip is also possible, but to account for the measured distribution of breakout width generally requires UCS much larger than currently estimated from the preliminary model of *in situ* rock strength derived from the single laboratory measurement of welded tuffs from Newberry, a review of the literature, and neutron porosity at depth. The occurrence of breakouts also requires a significant difference between  $S_{hmin}$  and  $S_{Hmax}$ , that suggests fractures that slip will have a strong tendency to strike nearly north-south which could impact the shape of the volume stimulated since previous studies in normal faulting regimes with this characteristic have shown a strong tendency for stimulation to extend in the direction of S<sub>Hmax</sub> by following the strike of highly stressed fractures (e.g., Heffer, 2002; Valley and Evans, 2007). This is stoichastically evaluated at Newberry using AltaStim by Cladouhos et al. (2011a).

Detailed analysis of mineralogy, temperature logs to further refine the hydrology of the borehole, and additional analyses of the potential stress tensor are ongoing. In addition, we note that a related study on the dilation potential and history of natural fracturing of core from Newberry borehole GEO N-2 (see Fetterman and Davatzes, 2011) is on-going as an independent, DOE-funded project (DOE grant DE- EE0002757).

## Acknowledgments

This study is based upon work supported by the Department of Energy under Award Number DE-EE0002777, with additional support provided by the USGS Energy Resources Program. We would like to acknowledge the support of AltaRock, Inc. for supporting this research, coordinating access to the site, and sharing borehole data with particular thanks to Trenton Cladouhos and Laura Nofziger. Dennis King and Joseph Svitek were critical to acquisition of the image log.

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